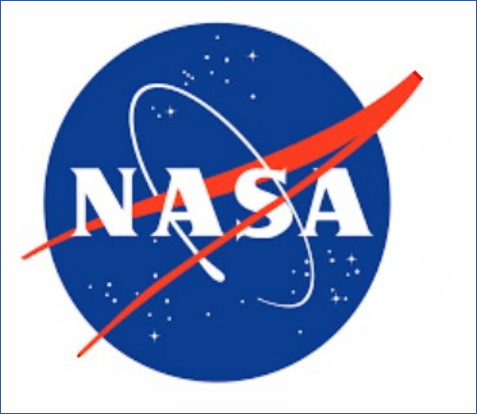


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NASA Technical Memorandum, mars 1972
Determination of Angles of Attack and Sideslip from Radar
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DETERMINATION OF ANGLES OF ATTACK
AND SIDESLIP FROM RADAR DATA
AND A ROLL-STABILIZED PLATFORM

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NASA Technical Memorandum, mars 1972
Determination of Angles of Attack and Sideslip from Radar Data and a Roll Stabilized Platform
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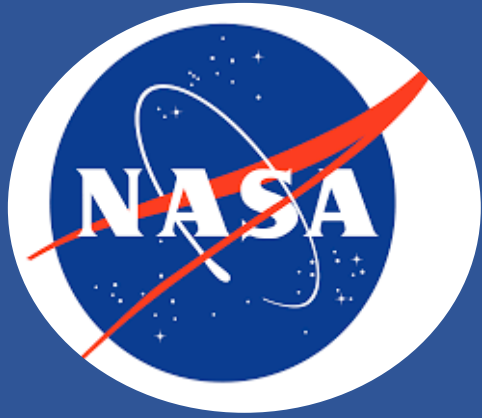


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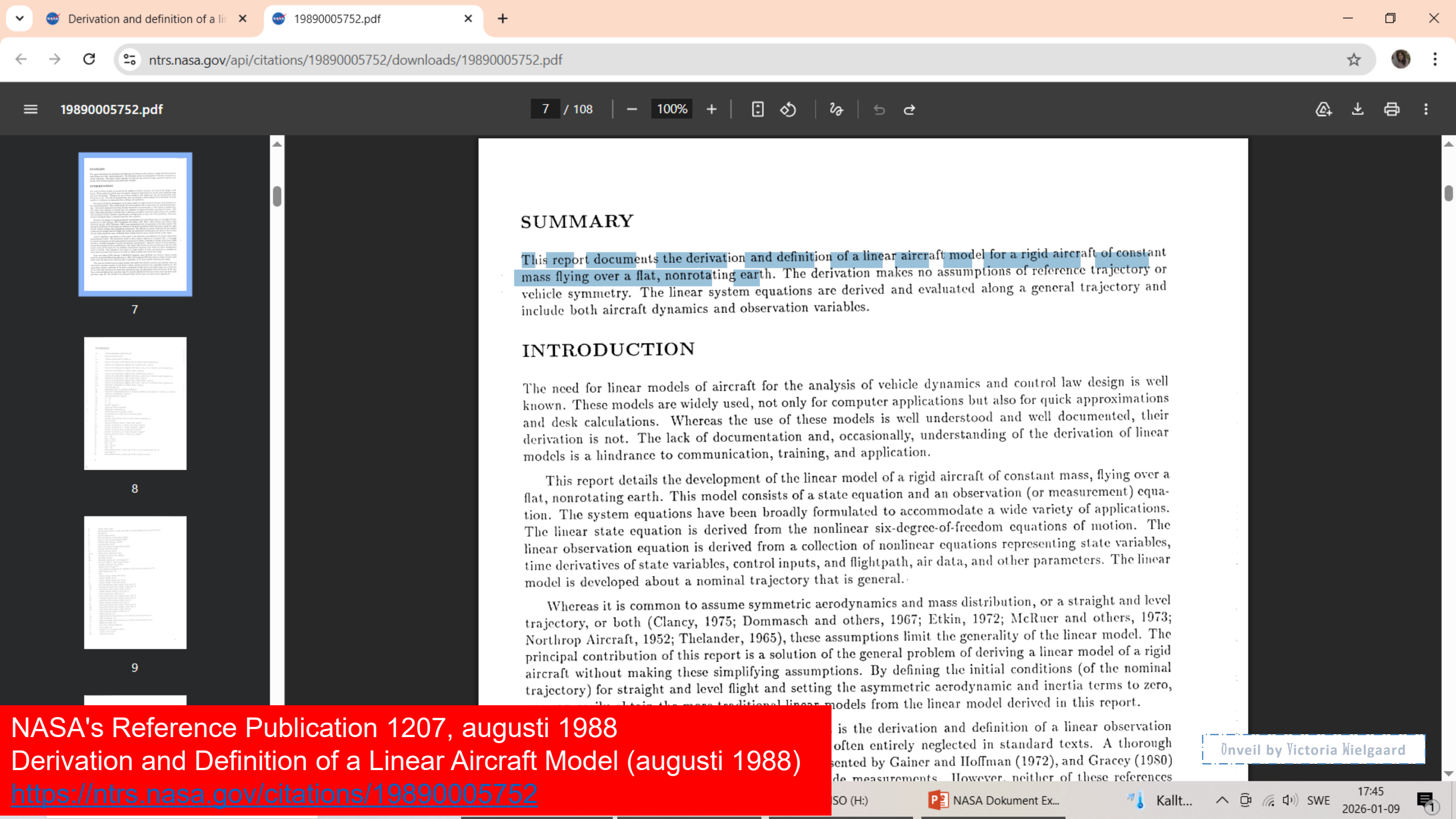


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1. Report No. NASA TM X-2514		2. Government Accession No.	3. Recipient's Catalog No. 0151793
4. Title and Subtitle DETERMINATION OF ANGLES OF ATTACK AND SIDESLIP FROM RADAR DATA AND A ROLL-STABILIZED PLATFORM		5. Report Date March 1972	6. Performing Organization Code
		8. Performing Organization Report No. L-7886	10. Work Unit No. 117-07-04-01
7. Author(s) John S. Preisser		11. Contract or Grant No.	
9. Performing Organization Name and Address NASA Langley Research Center Hampton, Va. 23365		13. Type of Report and Period Covered Technical Memorandum	
		14. Sponsoring Agency Code	
12. Sponsoring Agency Name and Address National Aeronautics and Space Administration Washington, D.C. 20546			
15. Supplementary Notes			
16. Abstract <p>Equations for angles of attack and sideslip relative to both a rolling and nonrolling body axis system are derived for a flight vehicle for which radar and gyroscopic-attitude data are available. The method is limited, however, to application where a flat, nonrotating earth may be assumed. The gyro considered measures attitude relative to an inertial reference in an Euler angle sequence. In particular, a pitch, yaw, and roll sequence is used as an example in the derivation. Sample calculations based on flight data are presented to illustrate the method. Results obtained with the present gyro method are compared with another technique that uses onboard-camera data.</p>			



NASA's Reference Publication 1207, augusti 1988
Derivation and Definition of a Linear Aircraft Model (augusti 1988)
<https://ntrs.nasa.gov/citations/19890005752>



SUMMARY

This report documents the derivation and definition of a linear aircraft model for a rigid aircraft of constant mass flying over a flat, nonrotating earth. The derivation makes no assumptions of reference trajectory or vehicle symmetry. The linear system equations are derived and evaluated along a general trajectory and include both aircraft dynamics and observation variables.

INTRODUCTION

The need for linear models of aircraft for the analysis of vehicle dynamics and control law design is well known. These models are widely used, not only for computer applications but also for quick approximations and desk calculations. Whereas the use of these models is well understood and well documented, their derivation is not. The lack of documentation and, occasionally, understanding of the derivation of linear models is a hindrance to communication, training, and application.

This report details the development of the linear model of a rigid aircraft of constant mass, flying over a flat, nonrotating earth. This model consists of a state equation and an observation (or measurement) equation. The system equations have been broadly formulated to accommodate a wide variety of applications. The linear state equation is derived from the nonlinear six-degree-of-freedom equations of motion. The linear observation equation is derived from a collection of nonlinear equations representing state variables, time derivatives of state variables, control inputs, and flightpath, air data, and other parameters. The linear model is developed about a nominal trajectory that is general.

Whereas it is common to assume symmetric aerodynamics and mass distribution, or a straight and level trajectory, or both (Clancy, 1975; Dommasch and others, 1967; Etkin, 1972; McRuer and others, 1973; Northrop Aircraft, 1952; Thelander, 1965), these assumptions limit the generality of the linear model. The principal contribution of this report is a solution of the general problem of deriving a linear model of a rigid aircraft without making these simplifying assumptions. By defining the initial conditions (of the nominal trajectory) for straight and level flight and setting the asymmetric aerodynamic and inertia terms to zero, the more traditional linear models from the linear model derived in this report.

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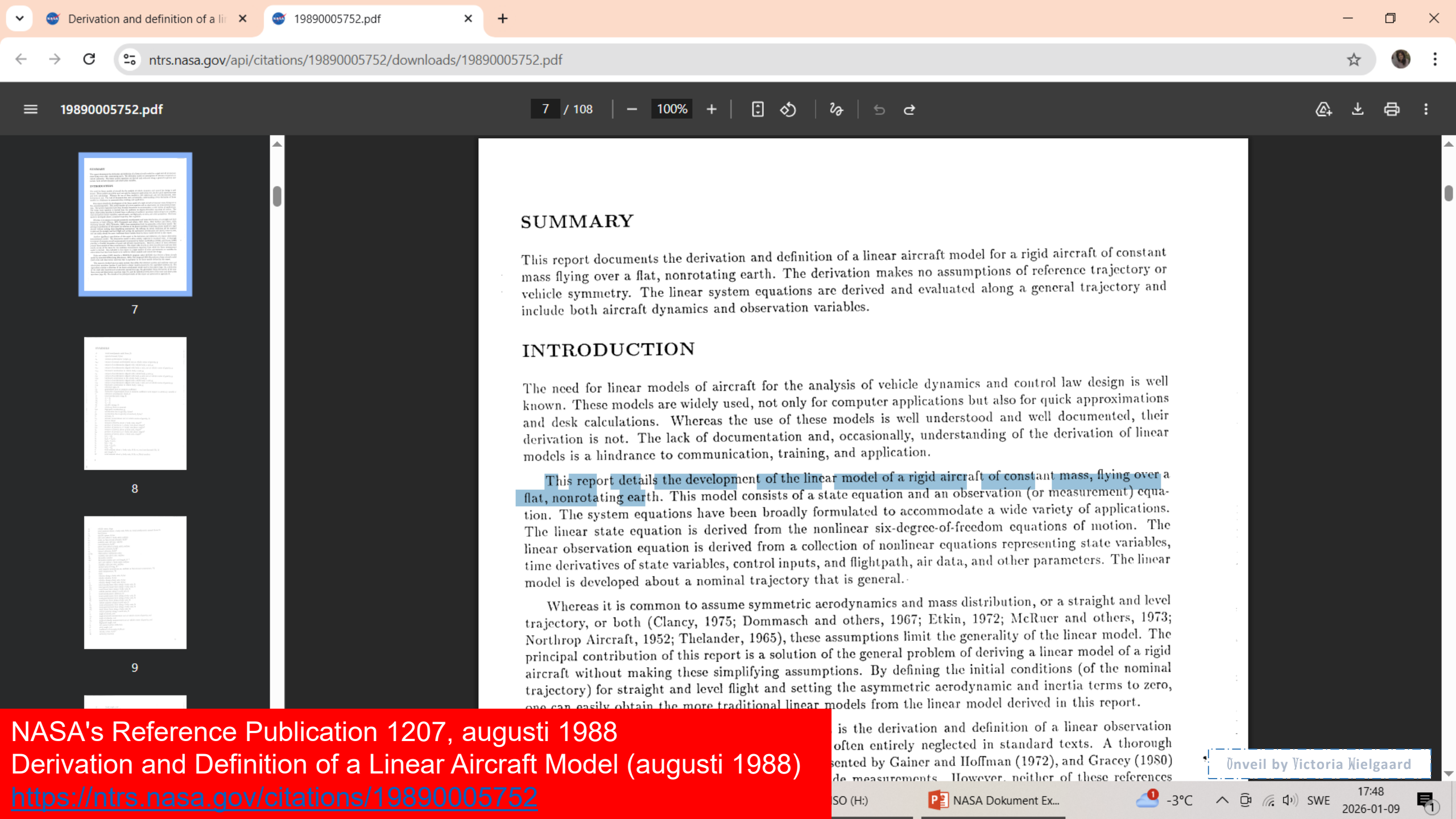
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SUMMARY

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INTRODUCTION

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$$C_{22} = \begin{bmatrix} 1.0 & -\partial(\dot{\alpha})/\partial \dot{V} & -\partial(\dot{\alpha})/\partial \dot{\alpha} & -\partial(\dot{\alpha})/\partial \dot{\beta} \\ -\partial(\dot{\alpha})/\partial \dot{V} & 1.0 & -\partial(\dot{\alpha})/\partial \dot{\alpha} & -\partial(\dot{\alpha})/\partial \dot{\beta} \\ -\partial(\dot{\beta})/\partial \dot{V} & -\partial(\dot{\beta})/\partial \dot{\alpha} & 1.0 & -\partial(\dot{\beta})/\partial \dot{\beta} \end{bmatrix}$$

$$= \begin{bmatrix} 1.0 (\bar{q} S \bar{c} / 2 V_0 m) (\cos \beta_0 C_{D_{\dot{\alpha}}} - \sin \beta_0 C_{Y_{\dot{\alpha}}}) & (\bar{q} S b / 2 V_0 m) (\cos \beta_0 C_{D_{\dot{\beta}}}) \\ 0 & 1.0 + (\bar{q} S \bar{c} / 2 V_0^2 m \cos \beta_0) C_{L_{\dot{\alpha}}} & (\bar{q} S b / 2 V_0^2 m \cos \beta_0) C_{L_{\dot{\beta}}} \\ 0 & (\bar{q} S \bar{c} / 2 V_0^2 m) (\sin \beta_0 C_{D_{\dot{\alpha}}} + \cos \beta_0 C_{Y_{\dot{\alpha}}}) & 1.0 - (\bar{q} S b / 2 V_0^2 m) (\sin \beta_0 C_{D_{\dot{\beta}}} + \cos \beta_0 C_{Y_{\dot{\beta}}}) \end{bmatrix} \quad (2-63)$$

The inverse of the C matrix, C^{-1} , can be expressed as a partitioned matrix in terms of the matrix subpartitions of the C matrix as

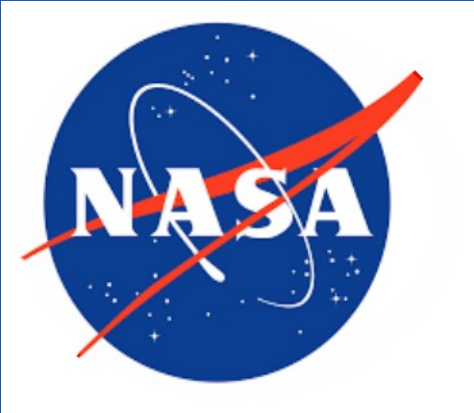
$$C^{-1} = \left[\begin{array}{c|c} C_{11}^{-1} & -C_{11}^{-1} C_{12} C_{22}^{-1} \\ \hline 0_{3 \times 3} & C_{22}^{-1} \end{array} \right] \begin{array}{c} 0_{6 \times 6} \\ \hline 1_{6 \times 6} \end{array} \quad (2-64)$$

The elements of the A' , B' , H' , and F' matrices can be determined using the C^{-1} matrix defined in equation (2-64), the A , B , H , G , and F matrices, and the definitions for A' , B' , H' , and F' given in equations (2-21), (2-22), (2-38), and (2-39).

3 CONCLUDING REMARKS

This report derives and defines a set of linearized system matrices for a rigid aircraft of constant mass, flying in a stationary atmosphere over a flat, nonrotating earth. Both generalized and standard linear system equations are derived from nonlinear six-degree-of-freedom equations of motion and a large collection of nonlinear observation (measurement) equations.

This derivation of a linear model is general and makes no assumptions on either the reference (nominal) trajectory about which the model is linearized or the symmetry of the vehicle mass and aerodynamic properties.



Dokument 20070030307

American Institute of Aeronautics and Astronautics

General Equations of Motion for a Damaged Asymmetric Aircraft.

<https://ntrs.nasa.gov/archive/nasa/casi.ntrs.nasa.gov/20070030307.pdf>




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General Equations of Motion for a Damaged Asymmetric Aircraft

There is a renewed interest in dynamic characteristics of damaged aircraft both in order to assess survivability and to develop control laws to enhance survivability. This paper presents a set of flight dynamics equations of motion for a rigid body not necessarily referenced to the body's center of mass. Such equations can be used when the body loses a portion of its mass and it is desired to track the motion of the body's previous center of mass/reference frame now that the mass center has moved to a new position. Furthermore, results for equations presented in this paper and equations in standard aircraft simulations are compared for a scenario involving a generic transport aircraft configuration subject to wing damage.

Document ID	20070030307
Acquisition Source	Langley Research Center
Document Type	Conference Paper
Authors	<div>Bacon, Barton J.</div> <div>(NASA Langley Research Center Hampton, VA, United States)</div> <div>Gregory, Irene M.</div> <div>(NASA Langley Research Center Hampton, VA, United States)</div>
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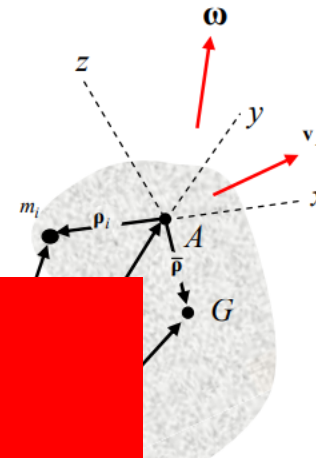
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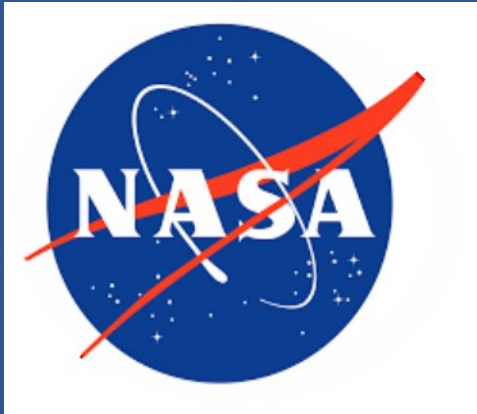
define angle of attack and sideslip angle, independent variables for the aerodynamic forces and moments. The proposed equations of motion are then applied to the problem of modeling large instantaneous shifts in center of mass of a rotating body that suddenly loses a portion of its mass. Benefits in simulation implementation are discussed. As an example, open loop dynamic responses of a generic transport aircraft with wing damage are compared for typical equations of motion used in the aircraft simulation and the equations presented here.

II. Rigid Body Equations of Motion Referenced to an Arbitrary Fixed Point on the Body

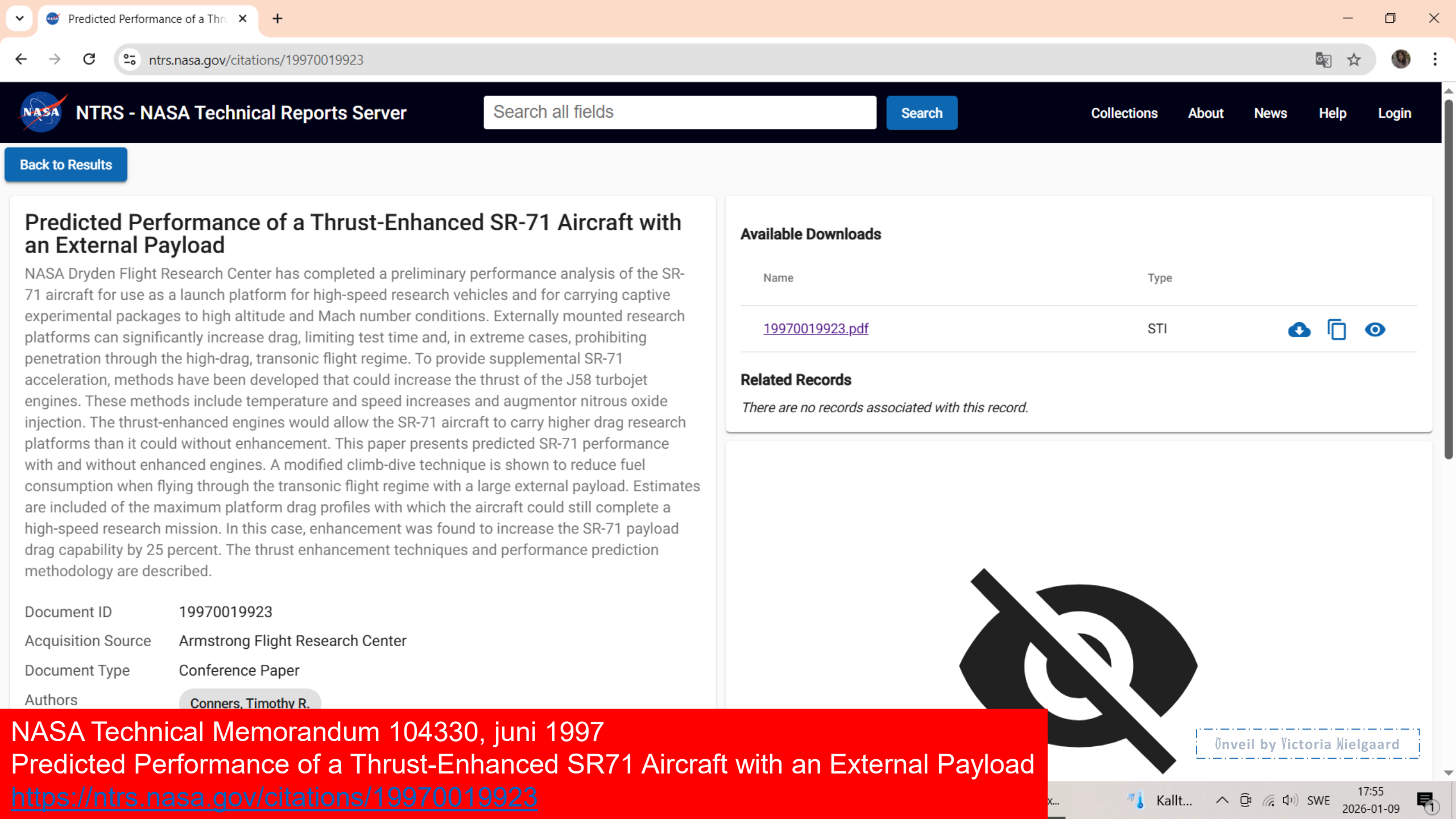
There are several approaches that can be used to develop the general equations of motion. The one selected here starts with Newton's laws applied to a collection of particles defining the rigid body (any number of dynamics or physics books can serve as references, e.g. reference 2). In this paper, the rigid body equations of motion over a flat non-rotating earth are developed that are not necessarily referenced to the body's center of mass. Such equations will be used in the next section when the body loses a portion of its mass and it is desired to track the motion of the body's previous center of mass/reference frame now that the mass center has moved to a new position



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NASA Technical Memorandum 104330, juni 1997
Predicted Performance of a Thrust-Enhanced SR71 Aircraft with an External Payload
<https://ntrs.nasa.gov/citations/19970019923>



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Predicted Performance of a Thrust-Enhanced SR-71 Aircraft with an External Payload

NASA Dryden Flight Research Center has completed a preliminary performance analysis of the SR-71 aircraft for use as a launch platform for high-speed research vehicles and for carrying captive experimental packages to high altitude and Mach number conditions. Externally mounted research platforms can significantly increase drag, limiting test time and, in extreme cases, prohibiting penetration through the high-drag, transonic flight regime. To provide supplemental SR-71 acceleration, methods have been developed that could increase the thrust of the J58 turbojet engines. These methods include temperature and speed increases and augmentor nitrous oxide injection. The thrust-enhanced engines would allow the SR-71 aircraft to carry higher drag research platforms than it could without enhancement. This paper presents predicted SR-71 performance with and without enhanced engines. A modified climb-dive technique is shown to reduce fuel consumption when flying through the transonic flight regime with a large external payload. Estimates are included of the maximum platform drag profiles with which the aircraft could still complete a high-speed research mission. In this case, enhancement was found to increase the SR-71 payload drag capability by 25 percent. The thrust enhancement techniques and performance prediction methodology are described.

Document ID 19970019923
Acquisition Source Armstrong Flight Research Center
Document Type Conference Paper
Authors Conners, Timothy R.

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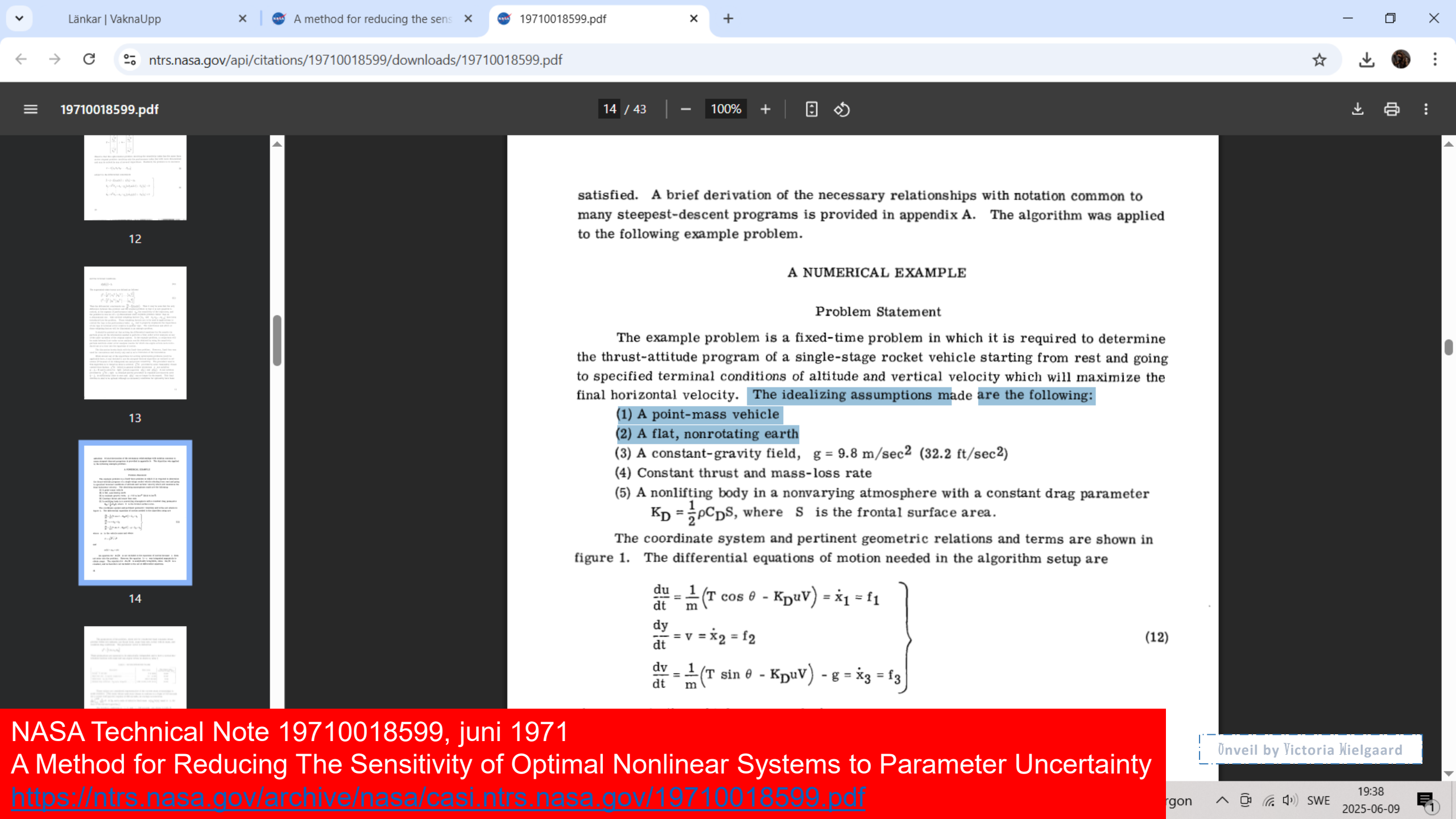
NASA Technical Memorandum 104330, juni 1997
Predicted Performance of a Thrust-Enhanced SR71 Aircraft with an External Payload
<https://ntrs.nasa.gov/citations/19970019923>



NASA Technical Note 19710018599, juni 1971

A Method for Reducing The Sensitivity of Optimal Nonlinear Systems to Parameter Uncertainty

<https://ntrs.nasa.gov/archive/nasa/casi.ntrs.nasa.gov/19710018599.pdf>



satisfied. A brief derivation of the necessary relationships with notation common to many steepest-descent programs is provided in appendix A. The algorithm was applied to the following example problem.

A NUMERICAL EXAMPLE

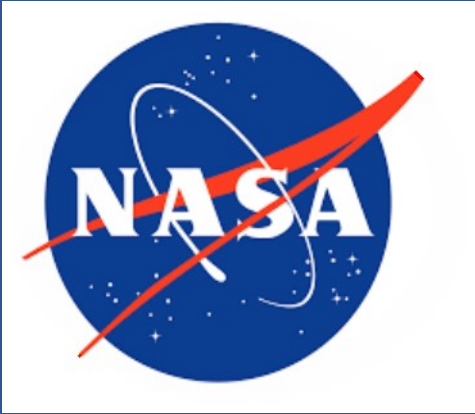
Problem Statement

The example problem is a fixed-time problem in which it is required to determine the thrust-attitude program of a single-stage rocket vehicle starting from rest and going to specified terminal conditions of altitude and vertical velocity which will maximize the final horizontal velocity. The idealizing assumptions made are the following:

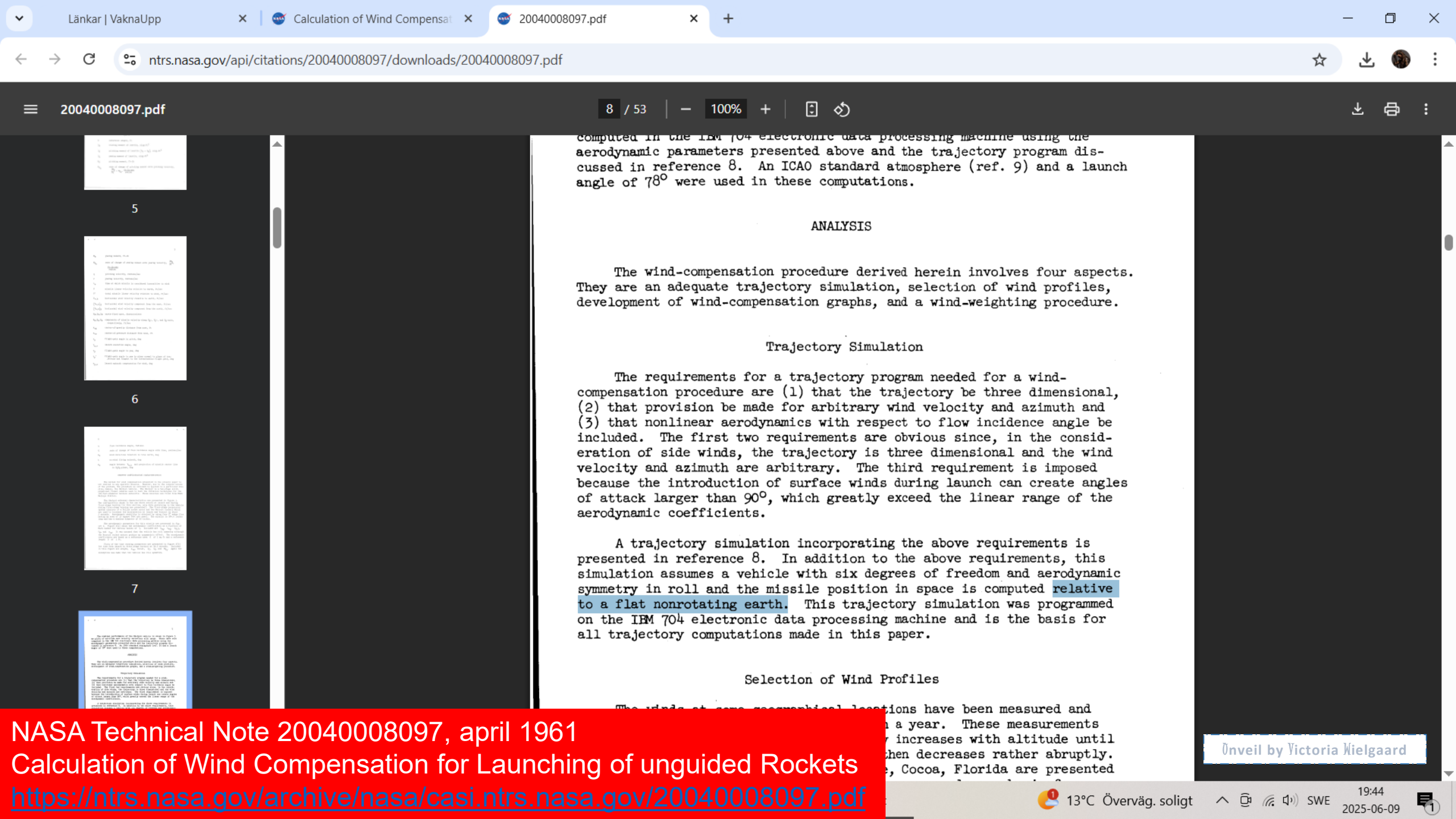
- (1) A point-mass vehicle
- (2) A flat, nonrotating earth
- (3) A constant-gravity field, $g = 9.8 \text{ m/sec}^2$ (32.2 ft/sec^2)
- (4) Constant thrust and mass-loss rate
- (5) A nonlifting body in a nonvarying atmosphere with a constant drag parameter $K_D = \frac{1}{2} \rho C_D S$, where S is the frontal surface area.

The coordinate system and pertinent geometric relations and terms are shown in figure 1. The differential equations of motion needed in the algorithm setup are

$$\left. \begin{aligned} \frac{du}{dt} &= \frac{1}{m} (T \cos \theta - K_D u V) = \dot{x}_1 = f_1 \\ \frac{dy}{dt} &= v = \dot{x}_2 = f_2 \\ \frac{dv}{dt} &= \frac{1}{m} (T \sin \theta - K_D u V) - g = \dot{x}_3 = f_3 \end{aligned} \right\} \quad (12)$$



NASA Technical Note 20040008097, april 1961
Calculation of Wind Compensation for Launching of unguided Rockets
<https://ntrs.nasa.gov/archive/nasa/casi.ntrs.nasa.gov/20040008097.pdf>



computed in the IBM 704 electronic data processing machine using the aerodynamic parameters presented above and the trajectory program discussed in reference 8. An ICAO standard atmosphere (ref. 9) and a launch angle of 78° were used in these computations.

ANALYSIS

The wind-compensation procedure derived herein involves four aspects. They are an adequate trajectory simulation, selection of wind profiles, development of wind-compensation graphs, and a wind-weighting procedure.

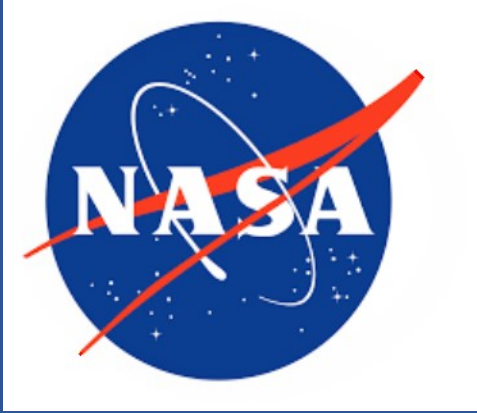
Trajectory Simulation

The requirements for a trajectory program needed for a wind-compensation procedure are (1) that the trajectory be three dimensional, (2) that provision be made for arbitrary wind velocity and azimuth and (3) that nonlinear aerodynamics with respect to flow incidence angle be included. The first two requirements are obvious since, in the consideration of side winds, the trajectory is three dimensional and the wind velocity and azimuth are arbitrary. The third requirement is imposed because the introduction of surface winds during launch can create angles of attack larger than 90° , which greatly exceed the linear range of the aerodynamic coefficients.

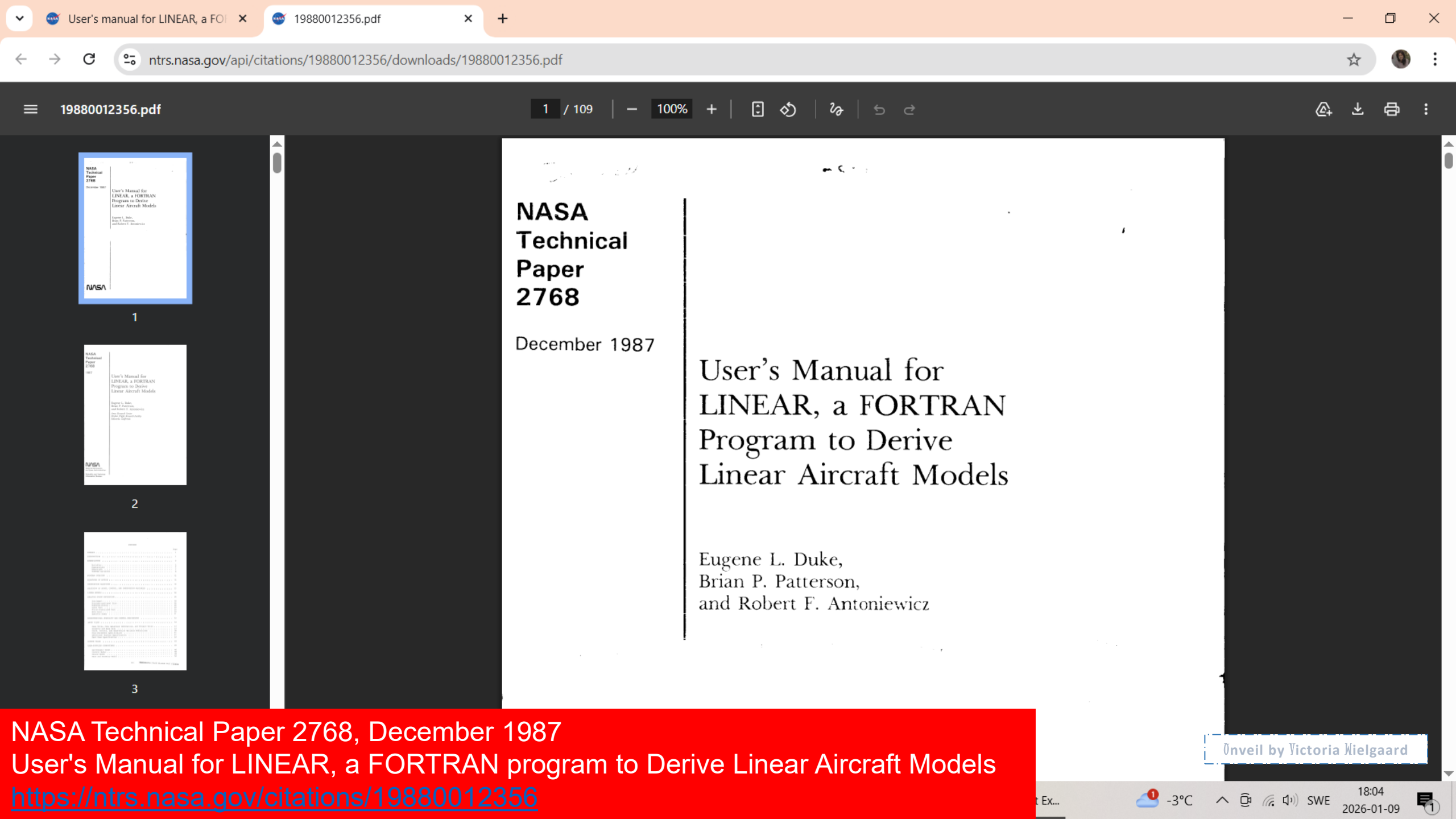
A trajectory simulation incorporating the above requirements is presented in reference 8. In addition to the above requirements, this simulation assumes a vehicle with six degrees of freedom and aerodynamic symmetry in roll and the missile position in space is computed relative to a flat nonrotating earth. This trajectory simulation was programmed on the IBM 704 electronic data processing machine and is the basis for all trajectory computations made in this paper.

Selection of Wind Profiles

The winds at some geographical locations have been measured and a year. These measurements increases with altitude until then decreases rather abruptly. e, Cocoa, Florida are presented



NASA Technical Paper 2768, December 1987
User's Manual for LINEAR, a FORTRAN program to Derive Linear Aircraft Models
<https://ntrs.nasa.gov/citations/19880012356>



NASA Technical Paper 2768

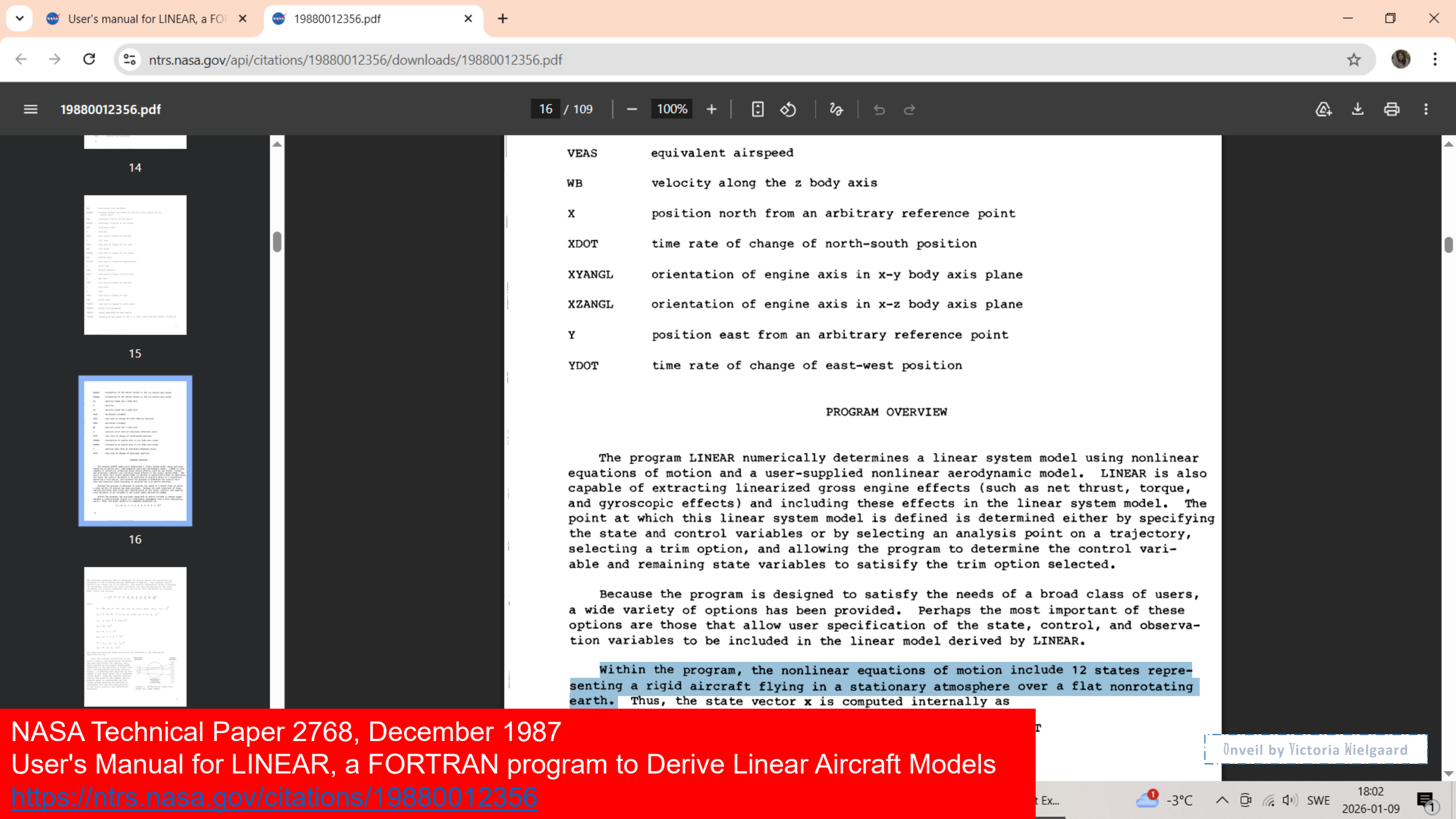
December 1987

User's Manual for LINEAR, a FORTRAN Program to Derive Linear Aircraft Models

Eugene L. Duke,
Brian P. Patterson,
and Robert F. Antoniewicz

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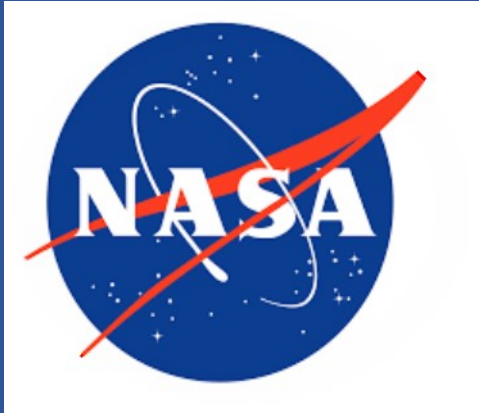
VEAS	equivalent airspeed
WB	velocity along the z body axis
X	position north from an arbitrary reference point
XDOT	time rate of change of north-south position
XYANGL	orientation of engine axis in x-y body axis plane
XZANGL	orientation of engine axis in x-z body axis plane
Y	position east from an arbitrary reference point
YDOT	time rate of change of east-west position

PROGRAM OVERVIEW

The program LINEAR numerically determines a linear system model using nonlinear equations of motion and a user-supplied nonlinear aerodynamic model. LINEAR is also capable of extracting linearized gross engine effects (such as net thrust, torque, and gyroscopic effects) and including these effects in the linear system model. The point at which this linear system model is defined is determined either by specifying the state and control variables or by selecting an analysis point on a trajectory, selecting a trim option, and allowing the program to determine the control variable and remaining state variables to satisfy the trim option selected.

Because the program is designed to satisfy the needs of a broad class of users, a wide variety of options has been provided. Perhaps the most important of these options are those that allow user specification of the state, control, and observation variables to be included in the linear model derived by LINEAR.

Within the program, the nonlinear equations of motion include 12 states representing a rigid aircraft flying in a stationary atmosphere over a flat nonrotating earth. Thus, the state vector x is computed internally as



NASA Technical Paper 2835, september 1988
User's Manual for LINEAR, a FORTRAN Program to Derive Linear Aircraft Models
<https://ntrs.nasa.gov/archive/nasa/casi.ntrs.nasa.gov/19890007066.pdf>

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An interactive FORTRAN program that provides the user with a powerful and flexible tool for the linearization of aircraft aerodynamic models is documented in this report. The program LINEAR numerically determines a linear system model using nonlinear equations of motion and a user-supplied linear or nonlinear aerodynamic model. The nonlinear equations of motion used are six-degree-of-freedom **equations with stationary atmosphere and flat, nonrotating earth assumptions.** The system model determined by LINEAR consists of matrices for both the state and observation equations. The program has been designed to allow easy selection and definition of the state, control, and observation variables to be used in a particular model.

Acquisition Source	Legacy CDMS
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Document Type Technical Publication (TP)

Authors **Antoniewicz, Robert F.**

(NASA Hugh L. Dryden Flight Research Facility Edwards, CA, United States)

Duke, Eugene L.

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User's Manual for Interactive LINEAR, a FORTRAN Program To Derive Linear Aircraft Models

Robert F. Antoniewicz,
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and Brian P. Patterson
*Ames Research Center
Dryden Flight Research Facility*

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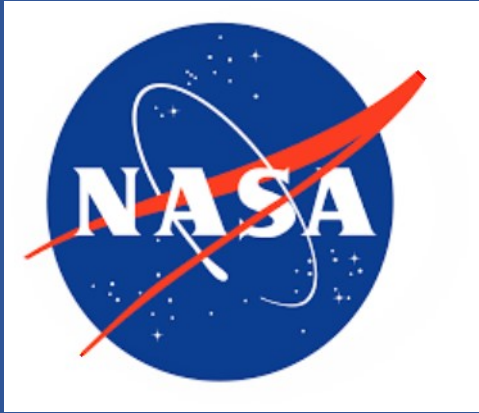
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12. Sponsoring Agency Name and Address National Aeronautics and Space Administration Washington, DC 20546		14. Sponsoring Agency Code	
15. Supplementary Notes A listing of the program Interactive LINEAR is provided in the microfiche supplement included with this report (4 sheets total).			
16. Abstract An interactive FORTRAN program that provides the user with a powerful and flexible tool for the linearization of aircraft aerodynamic models is documented in this report. The program LINEAR numerically determines a linear system model using nonlinear equations of motion and a user-supplied linear or nonlinear aerodynamic model. The nonlinear equations of motion used are six-degree-of-freedom equations with stationary atmosphere and flat, nonrotating earth assumptions. The system model determined by LINEAR consists of matrices for both the state and observation equations. The program has been designed to allow easy selection and definition of the state, control, and observation variables to be used in a particular model.			
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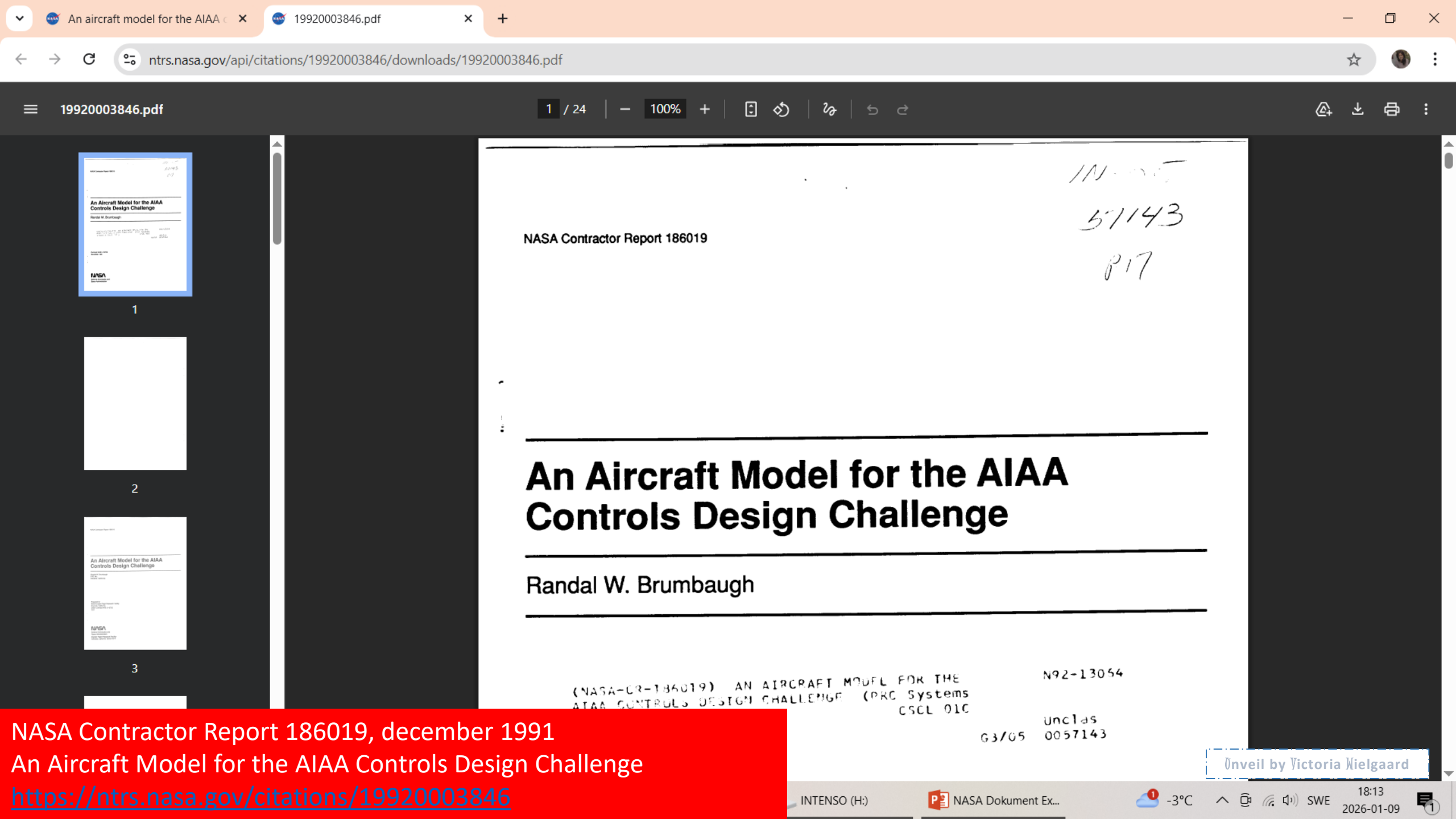
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NASA Contractor Report 186019

An Aircraft Model for the AIAA Controls Design Challenge

Randal W. Brumbaugh

(NASA-CR-186019) AN AIRCRAFT MODEL FOR THE
AIAA CONTROLS DESIGN CHALLENGE (PRC Systems
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An Aircraft Model for the AIAA Controls Design Challenge

Randal W. Brumbaugh
PRC Inc.,
Edwards, California

Prepared for
NASA Dryden Flight Research Facility
Edwards, California
Under Contract NAS 2-12722
1991

NASA
National Aeronautics and
Space Administration
Dryden Flight Research Facility
Edwards, California 93523-0273

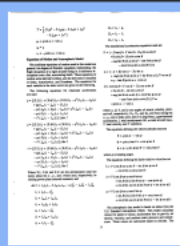
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13



14



15



$$T = \frac{1}{2} (I_x p^2 - 2 I_{xy} p q - 2 I_{xz} p r + I_y q^2 - 2 I_{yz} q r + I_z r^2)$$

$$p_s = p \cos \alpha + r \sin \alpha$$

$$q_s = q$$

$$r_s = -p \sin \alpha + r \cos \alpha$$

Equations of Motion and Atmospheric Model

The nonlinear equations of motion used in this model are general six-degree-of-freedom equations representing the flight dynamics of a rigid aircraft flying in a stationary atmosphere over a flat, nonrotating Earth. These equations of motion were derived by Etken, and the derivation is detailed in Duke, Antoniewicz, and Krambeer. The equations for each variable in the state vector are given in the following.

The following equations for rotational acceleration are used

$$\dot{p} = [(\Sigma L) I_1 + (\Sigma M) I_2 + (\Sigma N) I_3 - p^2 (I_{xx} I_2 - I_{xy} I_3) + pq (I_{xx} I_1 - I_{yz} I_2 - D_s I_3) - pr (I_{xy} I_1 + D_y I_2 - I_{yz} I_3) + q^2 (I_{yz} I_1 - I_{xy} I_3) - qr (D_x I_1 - I_{xy} I_2 + I_{xz} I_3) - r^2 (I_{yz} I_1 - I_{xz} I_2)] / \det I$$

$$\dot{q} = [(\Sigma L) I_2 + (\Sigma M) I_4 + (\Sigma N) I_5 - p^2 (I_{xx} I_4 - I_{xy} I_5) + pq (I_{xx} I_2 - I_{yz} I_4 - D_s I_5) - pr (I_{xy} I_2 + D_y I_4 - I_{yz} I_5) + q^2 (I_{yz} I_2 - I_{xy} I_5) - qr (D_x I_2 - I_{xy} I_4 + I_{xz} I_5) - r^2 (I_{yz} I_2 - I_{xz} I_4)] / \det I$$

$$D_x = I_x - I_y$$

$$D_y = I_x - I_z$$

$$D_z = I_y - I_z$$

The translational acceleration equations used are

$$\dot{V} = [-D \cos \beta + Y \sin \beta + X_T \cos \alpha \cos \beta + Y_T \sin \beta + Z_T \sin \alpha \cos \beta - mg (\sin \theta \cos \alpha \cos \beta - \cos \theta \sin \phi \sin \beta - \cos \theta \cos \phi \sin \alpha \cos \beta)] / m$$

$$\dot{\alpha} = [-L + Z_T \cos \alpha - X_T \sin \alpha + mg (\cos \theta \cos \phi \cos \alpha + \sin \theta \sin \alpha)] / V m \cos \beta + q - \tan \beta (p \cos \alpha + r \sin \alpha)$$

$$\dot{\beta} = [D \sin \beta + Y \cos \beta - X_T \cos \alpha \sin \beta + Y_T \cos \beta - Z_T \sin \alpha \sin \beta + mg (\sin \theta \cos \alpha \sin \beta + \cos \theta \sin \phi \cos \beta - \cos \theta \cos \phi \sin \alpha \sin \beta)] / V m + p \sin \alpha - r \cos \alpha$$

where α , β , θ , and ϕ are angles of attack, sideslip, pitch, and roll, respectively; X_T , Y_T , and Z_T are thrust along the x -, y -, and z -body axes; and D is drag force, g gravitational acceleration, L total aerodynamic lift, m total aircraft mass, V total velocity, and Y sideforce.

The equations defining the vehicle attitude rates are

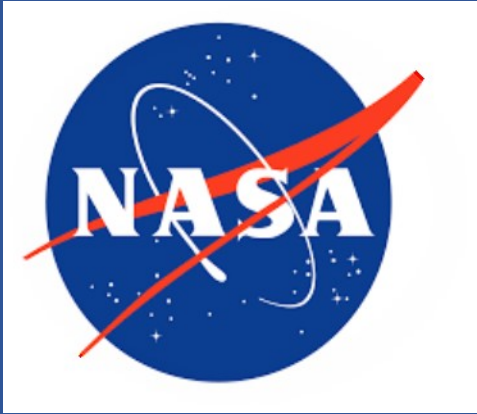
$$\dot{\theta} = q \cos \phi - r \sin \phi$$

$$\dot{\psi} = q \sin \phi \sec \theta + r \cos \phi \sec \theta$$

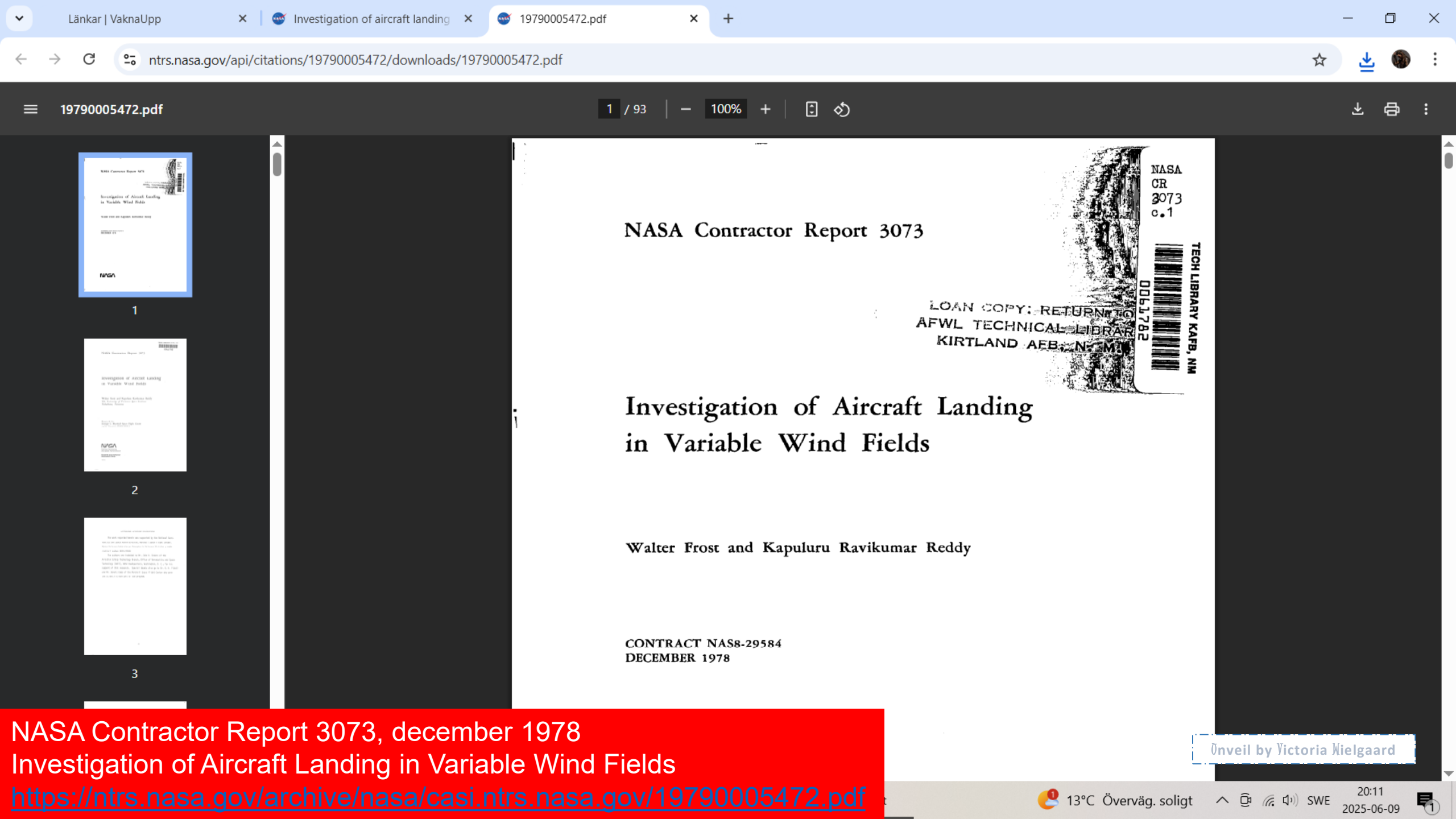
$$\dot{\phi} = p + q \sin \phi \tan \theta + r \cos \phi \tan \theta$$

where ψ is heading angle.

The equations defining the Earth-relative velocities are



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Investigation of Aircraft Landing
in Variable Wind Fields

Walter Frost and Kapuluru Ravikumar Reddy

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CHAPTER II

AIRCRAFT LANDING MODEL

1. Equations of Motion

The two-dimensional model for aircraft motion presented in this section follows the general form developed by Frost [12]. It accounts for both vertical and horizontal mean wind components having both time and spatial variations.

The aircraft trajectory model employed in this study was derived based on the following assumptions:

- a) The earth is flat and non-rotating.
- b) The acceleration of gravity, g , is constant (9.8 m/sec^2).
- c) Air density is constant (1.23 kg/m^3).
- d) The airframe is a rigid body.
- e) The aircraft is constrained to motion in the vertical plane.
- f) The aircraft has a symmetry plane (the x - z plane).
- g) The mass of the aircraft is constant.

re for steady-state flight.

acting on the aircraft. These

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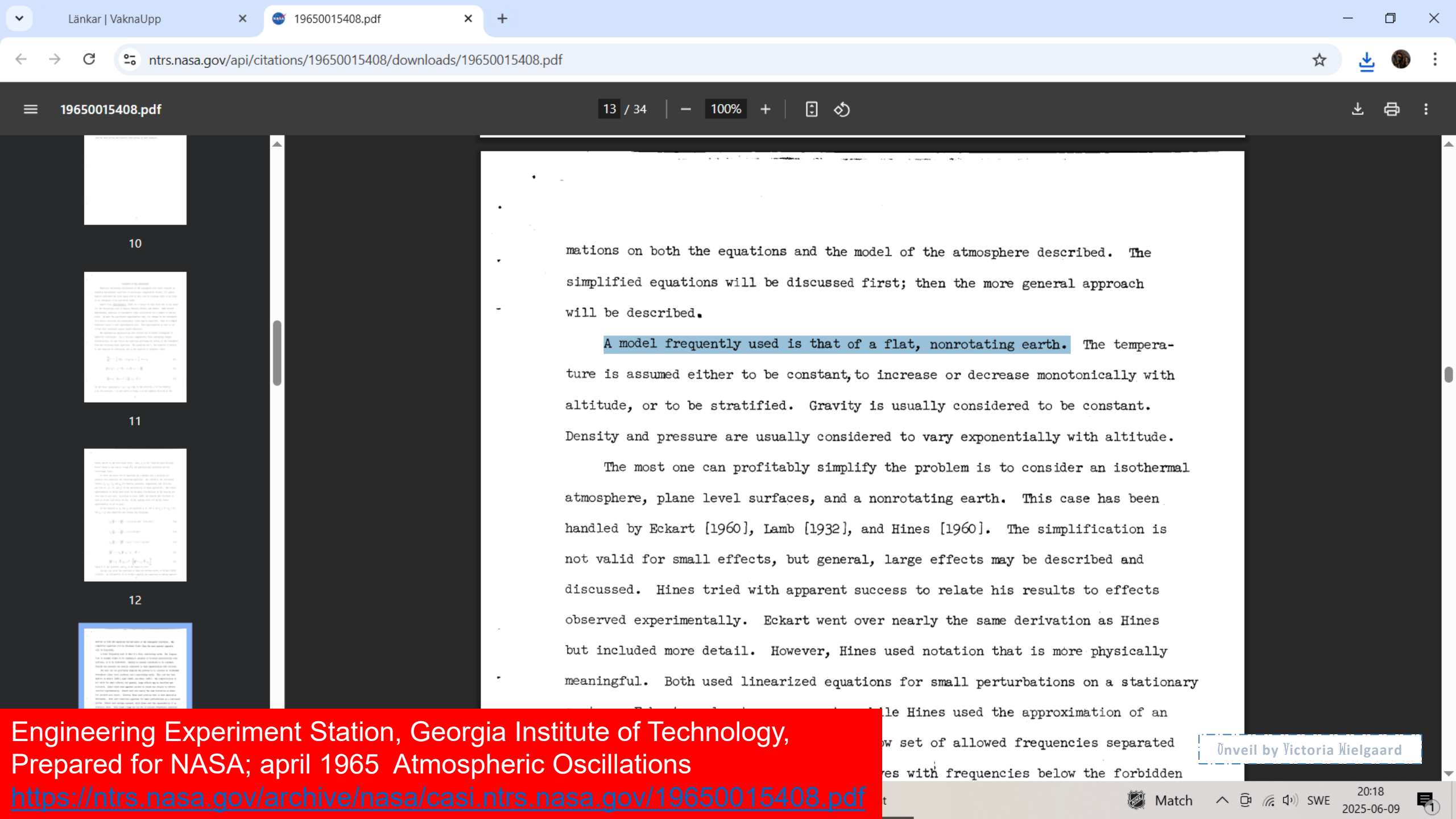
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mations on both the equations and the model of the atmosphere described. The simplified equations will be discussed first; then the more general approach will be described.

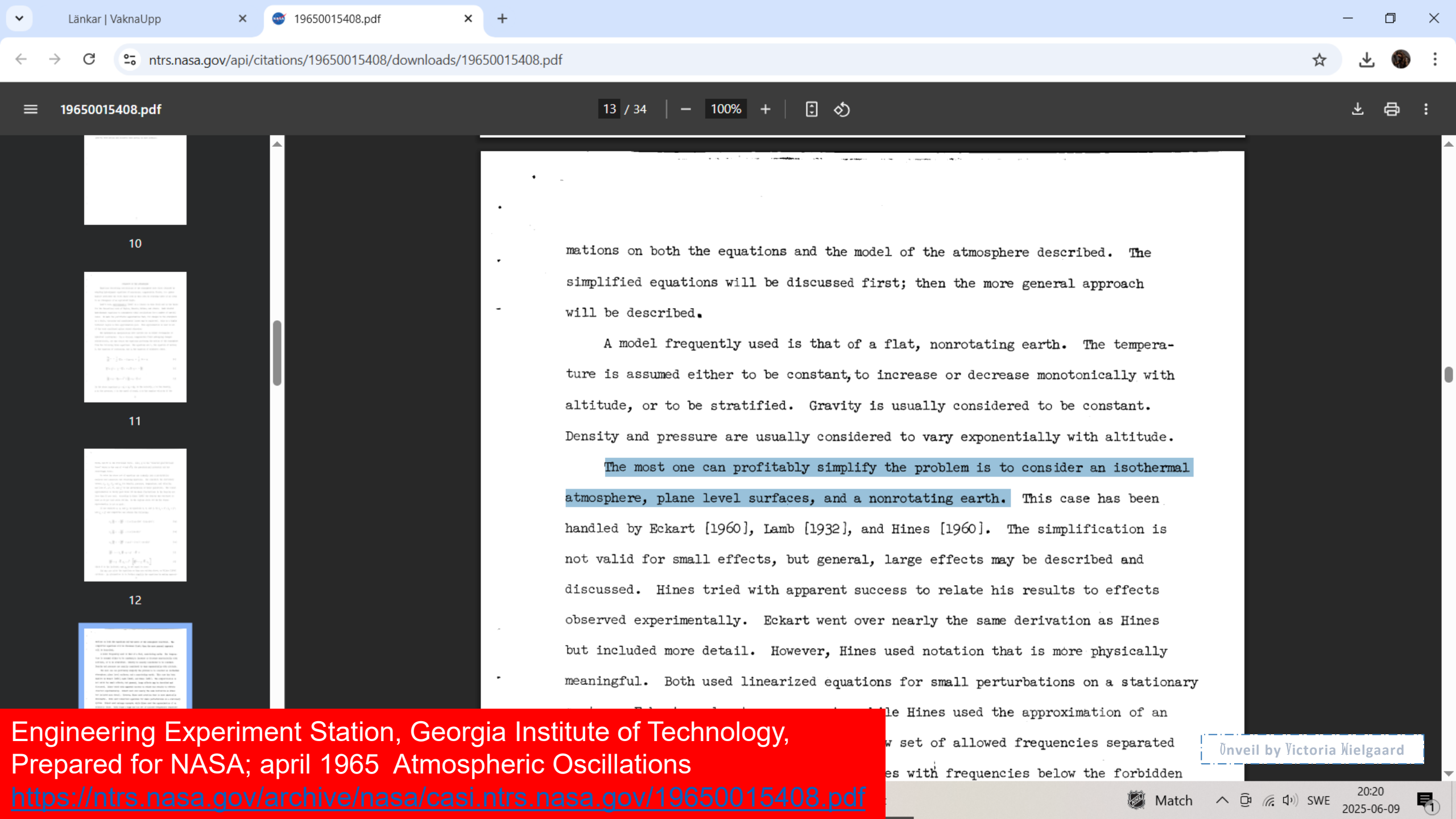
A model frequently used is that of a flat, nonrotating earth. The temperature is assumed either to be constant, to increase or decrease monotonically with altitude, or to be stratified. Gravity is usually considered to be constant. Density and pressure are usually considered to vary exponentially with altitude.

The most one can profitably simplify the problem is to consider an isothermal atmosphere, plane level surfaces, and a nonrotating earth. This case has been handled by Eckart [1960], Lamb [1932], and Hines [1960]. The simplification is not valid for small effects, but general, large effects may be described and discussed. Hines tried with apparent success to relate his results to effects observed experimentally. Eckart went over nearly the same derivation as Hines but included more detail. However, Hines used notation that is more physically meaningful. Both used linearized equations for small perturbations on a stationary

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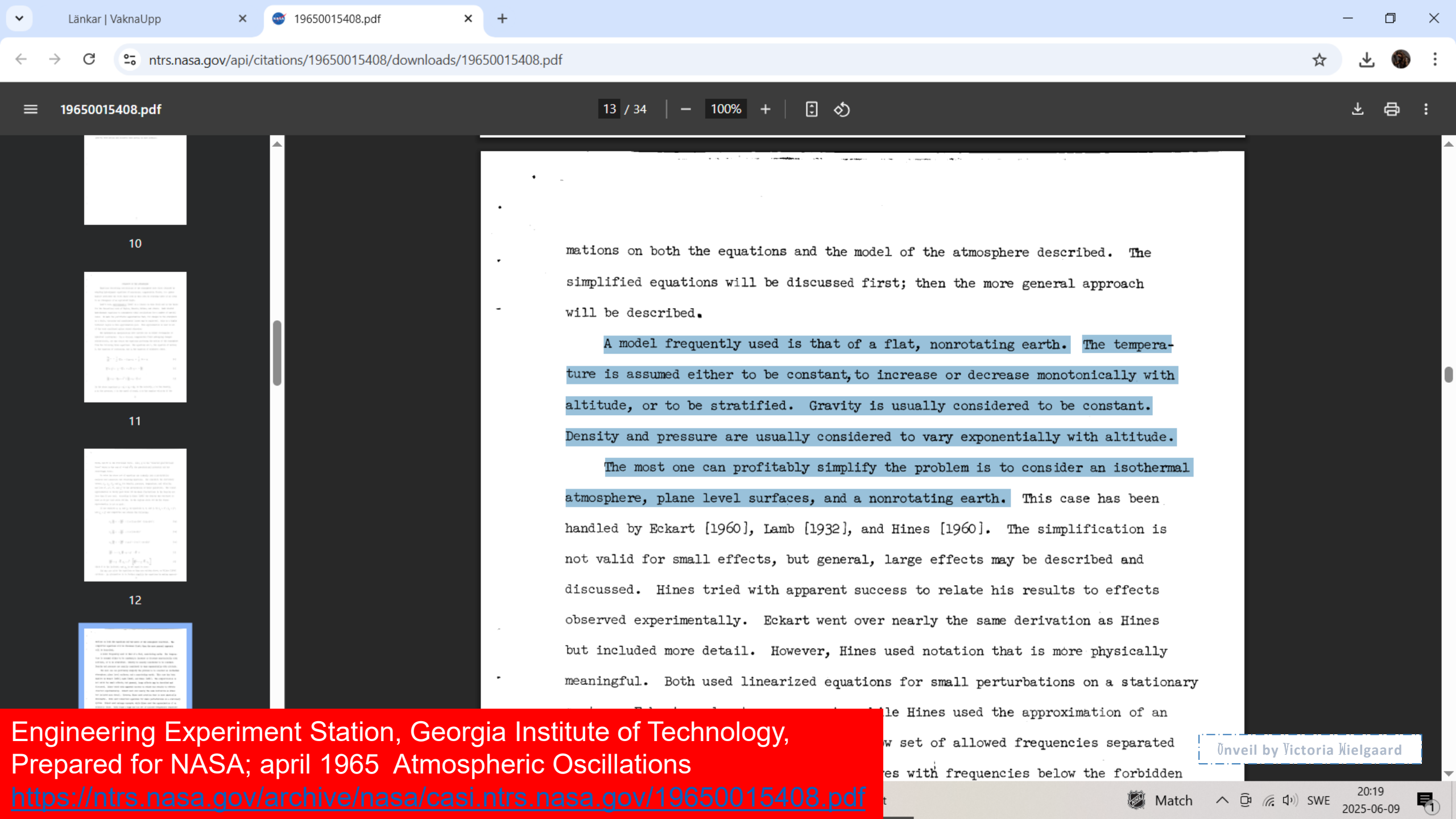
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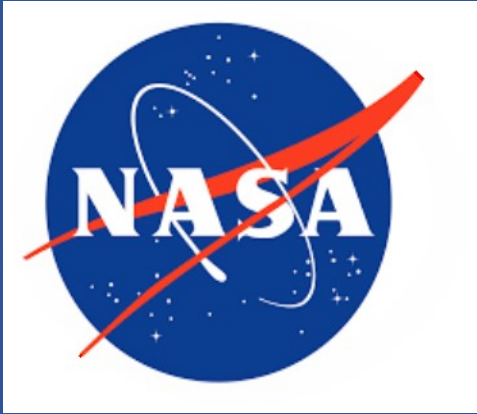
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NASA Technical Memorandum 81238, november 1980

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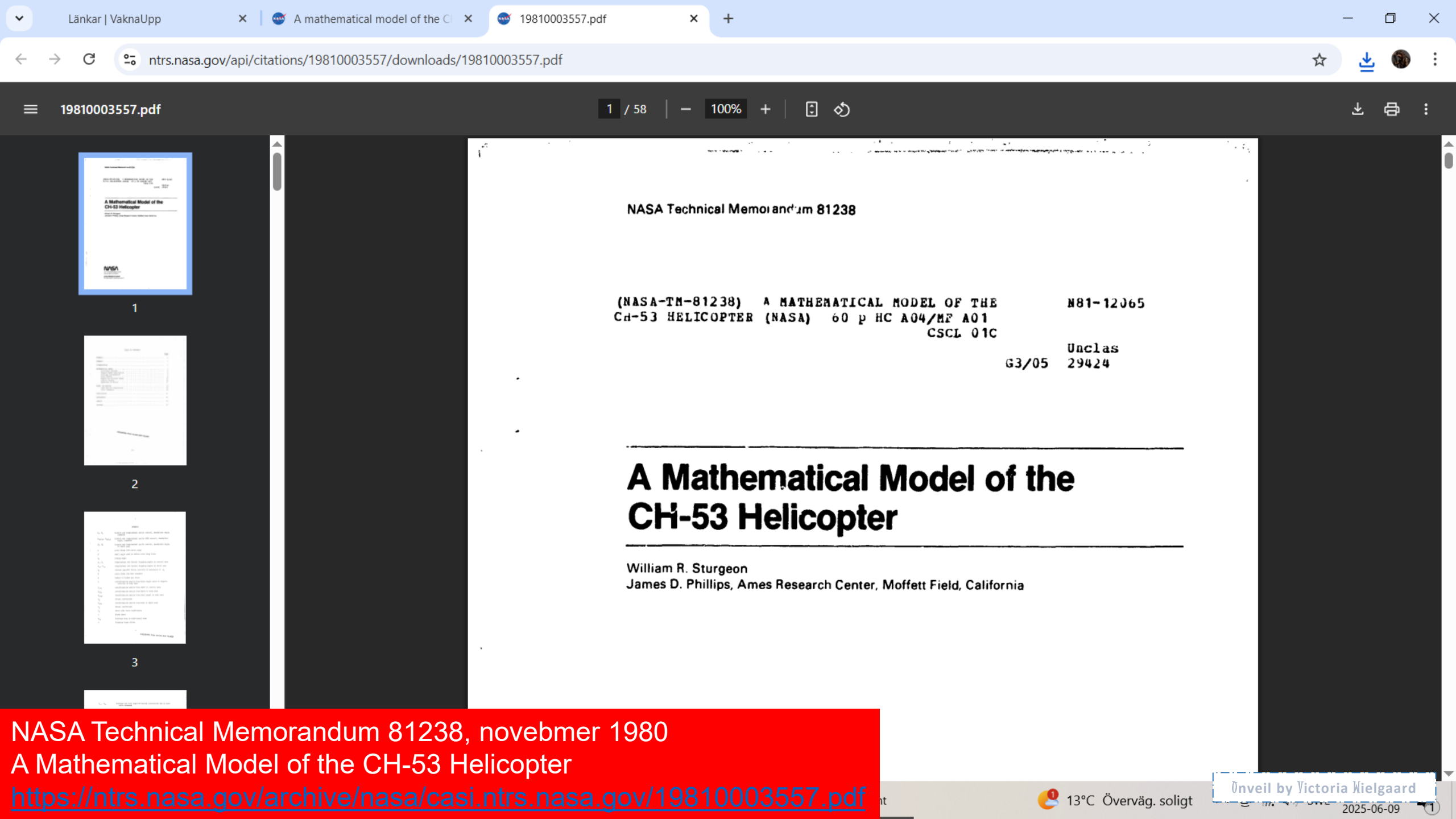
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A Mathematical Model of the CH-53 Helicopter

William R. Sturgeon
James D. Phillips, Ames Research Center, Moffett Field, California

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Equations of Motion

The helicopter equations of motion are given in body axes with respect to a flat, nonrotating Earth. The helicopter is considered a rigid body with mass symmetry about the $x_h - z_h$ plane. The effects due to the engine angular momentum are neglected.

Translational acceleration- The translational equations of motion are

$$C_{h/e} \begin{bmatrix} 0 \\ 0 \\ mg \end{bmatrix} + \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{f, h} + \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{r, h} = m \begin{bmatrix} \dot{u} \\ \dot{v} \\ \dot{w} \end{bmatrix}_{cg, h} + \begin{bmatrix} 0 & -r & q \\ r & 0 & -p \\ -q & p & 0 \end{bmatrix}_h \begin{bmatrix} u \\ v \\ w \end{bmatrix}_{cg, h} \quad (45)$$

where

$$C_{h/e} = \begin{bmatrix} \cos \theta \cos \psi & \cos \theta \sin \psi & -\sin \theta \\ \sin \phi \sin \theta \cos \psi & \cos \phi \cos \psi & \sin \phi \cos \theta \\ -\cos \phi \sin \psi & + \sin \phi \sin \theta \sin \psi & \\ \cos \phi \sin \theta \cos \psi & \cos \phi \sin \theta \sin \psi & \cos \phi \cos \theta \\ + \sin \phi \sin \psi & - \sin \phi \cos \psi & \end{bmatrix}_h \quad (46)$$

and ϕ_h , θ_h , and ψ_h are the Euler angles that define the orientation of the body axis system (fig. 3). The fuselage aerodynamic forces are given by equation (10), and the rotor forces, which include those due to both main and tail rotors, are given by equation (31). Equation (45) can be rearranged to yield

$$\begin{bmatrix} \dot{u} \\ \dot{v} \\ \dot{w} \end{bmatrix} = \frac{1}{m} \left[\begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{f, h} + \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{r, h} \right] - \begin{bmatrix} 0 & -r & q \\ r & 0 & -p \\ -q & p & 0 \end{bmatrix}_h \begin{bmatrix} u \\ v \\ w \end{bmatrix}_{cg, h} + C_{h/e} \begin{bmatrix} 0 \\ 0 \\ g \end{bmatrix} \quad (47)$$

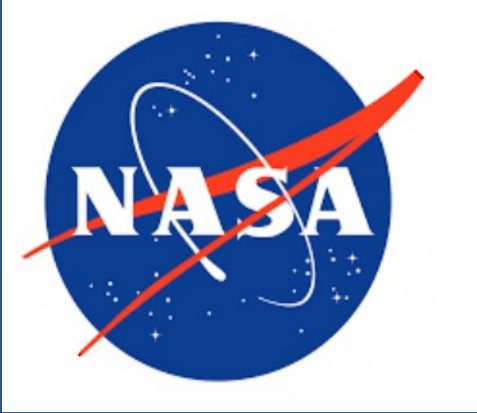
inertial velocity, in body coordi-

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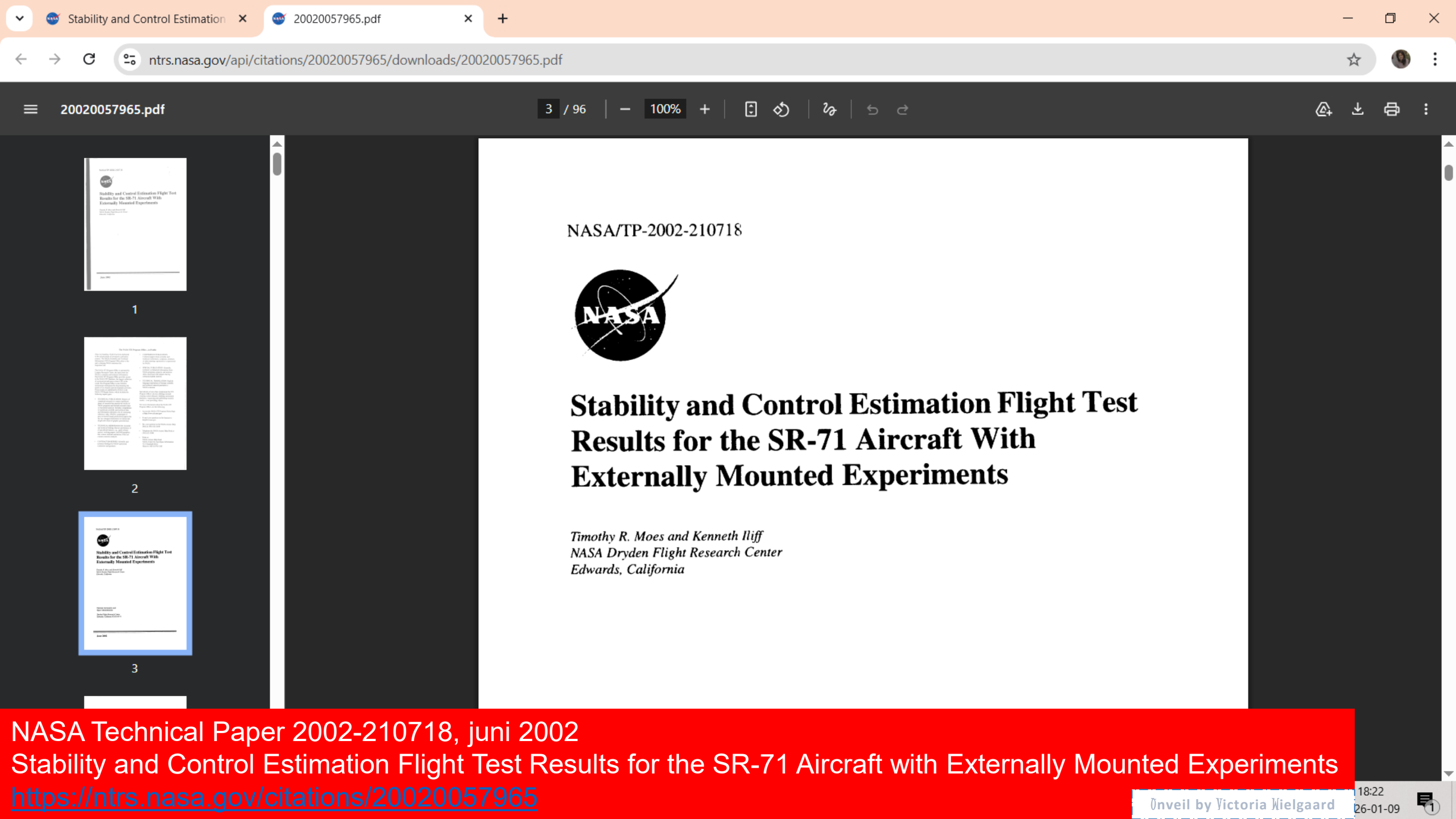
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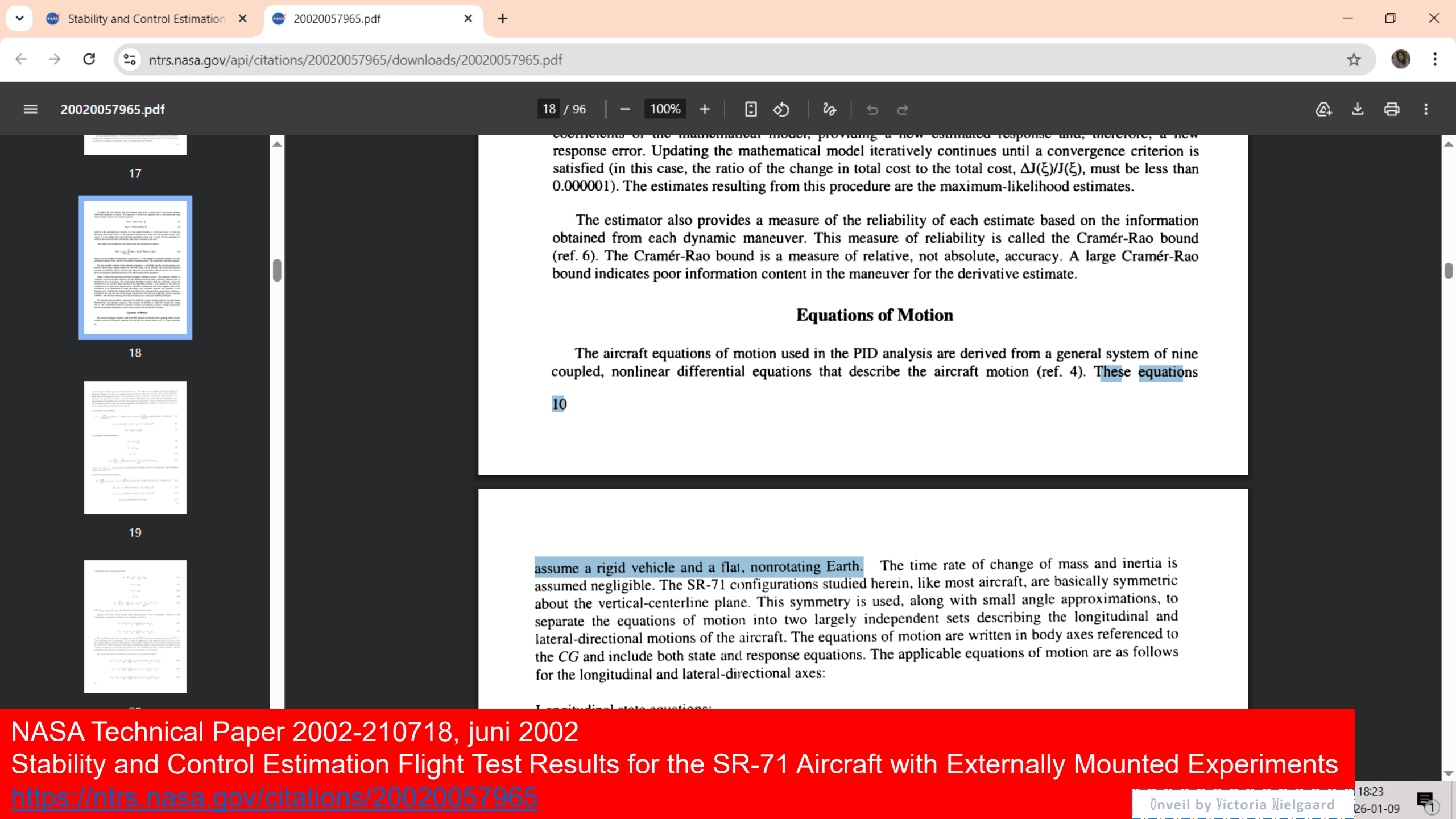
Stability and Control Estimation Flight Test Results for the SR-71 Aircraft With Externally Mounted Experiments

*Timothy R. Moes and Kenneth Iliff
NASA Dryden Flight Research Center
Edwards, California*

NASA Technical Paper 2002-210718, juni 2002
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coefficients of the mathematical model, providing a new estimated response and, therefore, a new response error. Updating the mathematical model iteratively continues until a convergence criterion is satisfied (in this case, the ratio of the change in total cost to the total cost, $\Delta J(\xi)/J(\xi)$, must be less than 0.000001). The estimates resulting from this procedure are the maximum-likelihood estimates.

The estimator also provides a measure of the reliability of each estimate based on the information obtained from each dynamic maneuver. This measure of reliability is called the Cramér-Rao bound (ref. 6). The Cramér-Rao bound is a measure of relative, not absolute, accuracy. A large Cramér-Rao bound indicates poor information content in the maneuver for the derivative estimate.

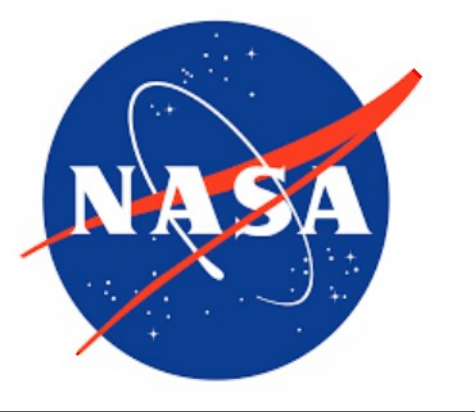
Equations of Motion

The aircraft equations of motion used in the PID analysis are derived from a general system of nine coupled, nonlinear differential equations that describe the aircraft motion (ref. 4). These equations

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assume a rigid vehicle and a flat, nonrotating Earth. The time rate of change of mass and inertia is assumed negligible. The SR-71 configurations studied herein, like most aircraft, are basically symmetric about the vertical-centerline plane. This symmetry is used, along with small angle approximations, to separate the equations of motion into two largely independent sets describing the longitudinal and lateral-directional motions of the aircraft. The equations of motion are written in body axes referenced to the CG and include both state and response equations. The applicable equations of motion are as follows for the longitudinal and lateral-directional axes:

Longitudinal state equations:



NASA Technical Memorandum 100996, maj 1988
Flight Testing a VSTOL Aircraft to Identify a Full-Envelope Aerodynamic Model.
<https://ntrs.nasa.gov/archive/nasa/casi.ntrs.nasa.gov/19880014378.pdf>

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as with the longitudinal maneuver. A wings-level rudder frequency sweep and a rudder-fixed aileron frequency sweep provide additional lateral-axis excitation. The pilot uses aileron control to hold the wings-level condition during the sideslip and the rudder sweep portions of the maneuver. An initial roll angle of 40° was chosen for the aileron sweep. Thrust is added at the end of the maneuver to return to the nominal trim point. Thirteen of these lateral maneuvers were performed.

Preliminary Processing

Following real-time acquisition of data during flight test, each recorded maneuver, with instrument calibrations added, is converted to engineering units and made available to researchers as a raw flight-data file. An interactive program called PRODAT (PROcess DATA) is used to read the raw flight-data file, identify wild points, and filter data records. Data are then stored in a "processed" file of selected channels at a submultiple of the main-frame sample rate. PRODAT runs on a VAX-8650. Processing begins by removing wild points from the records. Several methods are

State Estimation

The next step in the processing of each maneuver is to apply SMACK¹⁹⁻²¹ (SMoothing for AirCRAFT Kinematics), a state-estimation program developed at Ames Research Center, to check data consistency and derive unmeasured variables. SMACK runs on a Cray-XMP computer. State estimation in this paper refers to a process that solves a state model,

$$\dot{x} = f(x, w), \quad x(t_0) = x_0 \quad (2)$$

such that $h(x)$ in the measurement model

$$z = h(x) + v \quad (3)$$

suitably matches the data record over a time interval (t_0, t_f) , usually in a least-squares error sense.^{7,22} In Eq. (2), x is the state vector and w is a vector that represents unknown forcing functions (derivatives of unmeasured variables, e.g., angular accelerations). For aircraft problems, the state and measurement models together

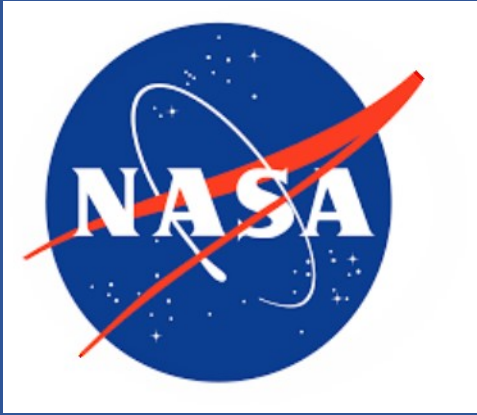
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represent the kinematics of a rigid body for describing motion over a flat, nonrotating Earth. In the SMACK formulation, the state model consists of Euler angles and position variables and their derivatives. When flightpath winds are to be identified, the state model is augmented by wind velocities and accelerations. The measurement model

measured in flight. It should be noted that the propulsion model provides only thrust forces and moments. Any thrust-induced aerodynamic effects are to be included in the VSRA aerodynamic model.

Inputs to the ENCAL routine include all the air-data, reaction control, engine, and weight data listed in Table 1. Outputs to the air-data file are the three body-axis engine forces and moments. ENCAL also includes aircraft weight and inertias, and center-of-gravity (c.g.) location. Variations are based on manufac-

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NASA Ames Research Center, januari 2006

Singular Arc Time-Optimal Climb Trajectory of Aircraft in a Two-Dimensional Wind Field

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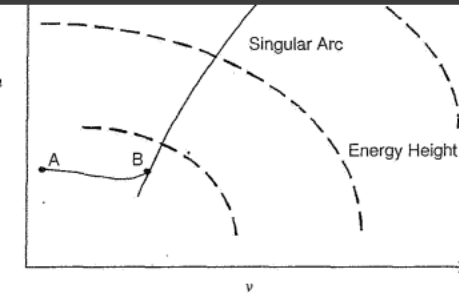


Fig. 1 - Time-Optimal Energy Climb Path

Within the framework of the Pontryagin's minimum principle, the singular-arc optimal control method is an intermediate method for the trajectory optimization. The existence of a singular arc in the time optimal control can simplify the trajectory optimization significantly. Briefly, the singular arc is described by a switching function that minimizes a Hamiltonian function when the Hamiltonian function is linear with respect to a control variable.

In this study, we will examine an aspect of the minimum time-to-climb problem for an aircraft flying in the presence of a two-dimensional atmospheric wind field. An analytical solution for the singular arc is obtained. Wind patterns at a local airport can affect the climb performance of aircraft. While the time-optimal climb problems have been thoroughly studied in flight mechanics, the effect of winds are usually not included in these studies. A solution method of a minimum-time to climb will then be presented for computing a minimum time-to-climb flight trajectory.

II. Singular Arc Optimal Control

In our minimum time-to-climb problem, the aircraft is modeled as a point mass and the flight trajectory is strictly confined in a vertical plane on a non-rotating, flat earth. The change in mass of the aircraft is neglected and the engine thrust vector is assumed to point in the direction of the aircraft velocity vector. In addition, the aircraft is assumed to fly in an atmospheric wind field comprising of both horizontal and vertical components that are altitude-dependent. The horizontal wind component normally comprises a longitudinal and lateral component. We assume that the aircraft motion is symmetric so that the lateral wind component is not included. Thus, the pertinent equations of motion for the problem are defined in its state variable form as

$$\dot{h} = v \sin \gamma + w_h \quad (1)$$

$$\dot{v} = \frac{T - D - W \sin \gamma}{m} - \dot{w}_x \cos \gamma - \dot{w}_h \sin \gamma \quad (2)$$

$$L - W \cos \gamma, \quad \dot{w}_x \sin \gamma - \dot{w}_h \cos \gamma \quad (3)$$